

Anomalous 5/2 Quantum Hall Phase Due to Landau-Level Mixing

Sudipto Das*, Sahana Das, and Sudhansu S. Mandal

Indian Institute of Technology Kharagpur, India

*Email: sudiptodas.cgr@gmail.com



INTRODUCTION

- ❖ Current carrying 2D electron gas subjected to high magnetic field at very low temperature
 - ⇒ Discretize Fermi sea ⇒ Landau levels
 - ⇒ Quantum Hall effect
- ❖ Filling factor, $\nu = N/N_\phi \Rightarrow$ Integer, Fraction
- ❖ $\nu = 5/2 \Rightarrow 1/2$ -filled second Landau level
 - ⇒ Enigmatic state
- ❖ $\nu = 5/2 \Rightarrow$ Hosts non-Abelian quasi-particle
 - ⇒ qubit of fault tolerant *Topological* quantum computer^[1]

- ❖ Topologically distinct possible candidates for 5/2,

Phases	Flux, N_ϕ	Model wave function	K
Pfaffian (Pf)	$2N - 3$	Moore-Read Pfaffian ^[2]	$7/2$
Anti-Pfaffian (A-Pf)	$2N + 1$	Moore-Read Conjugate	$5/2$
Particle-hole symmetric Pfaffian (PH-Pf)	$2N - 1$?	$3/2$

The Debate

Theoretical studies favour
⇒ A-Pf



Experimental observations favour^[3,4] ⇒ PH-Pf

LANDAU LEVEL MIXING THEORY

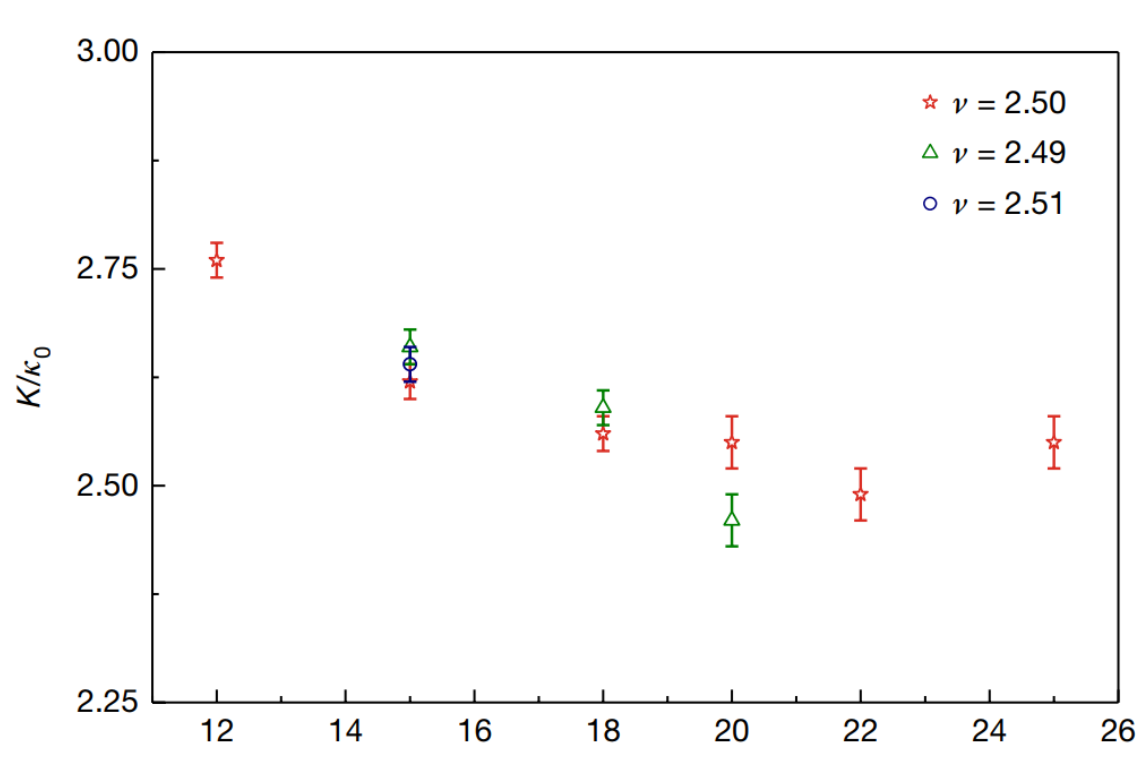
- ❖ 5/2 state observed at $\Rightarrow B \sim 12 - 1$ T
- ❖ For GaAs sample LLM strength, $\kappa \sim 0.7-2.5$ ($\kappa = 2.52/\sqrt{B}$)
- ❖ Theoretical predictions were limited to $\kappa \lesssim 1$
- ❖ The "realistic regime", $\kappa \gtrsim 1$ remained **UNEXPLORED !!**
- ❖ Effective Hamiltonian^[5],

$$\hat{H}_{\text{eff}}(\kappa) = \sum_m \left[V_m^{(2)} \Big|_{\text{Coulomb}} + \kappa \delta V_m^{(2)} \right] + \sum_m \kappa V_m^{(3)}$$

where $V_m^{(2)}$ and $V_m^{(3)}$ are two and three body m -th pseudopotentials respectively

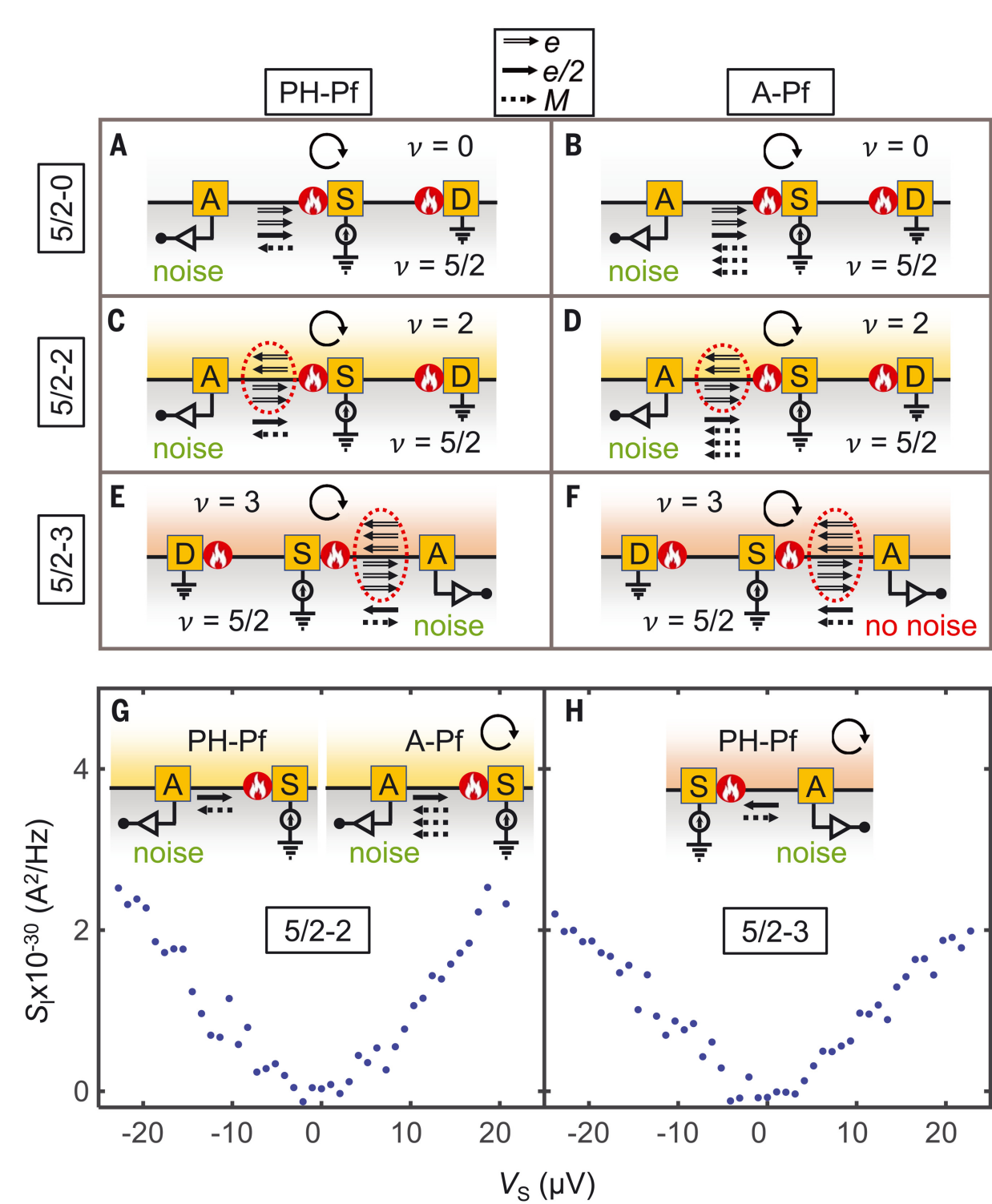
EXPERIMENTAL EVIDENCE

Thermal Hall Conductivity Measurement^[3]



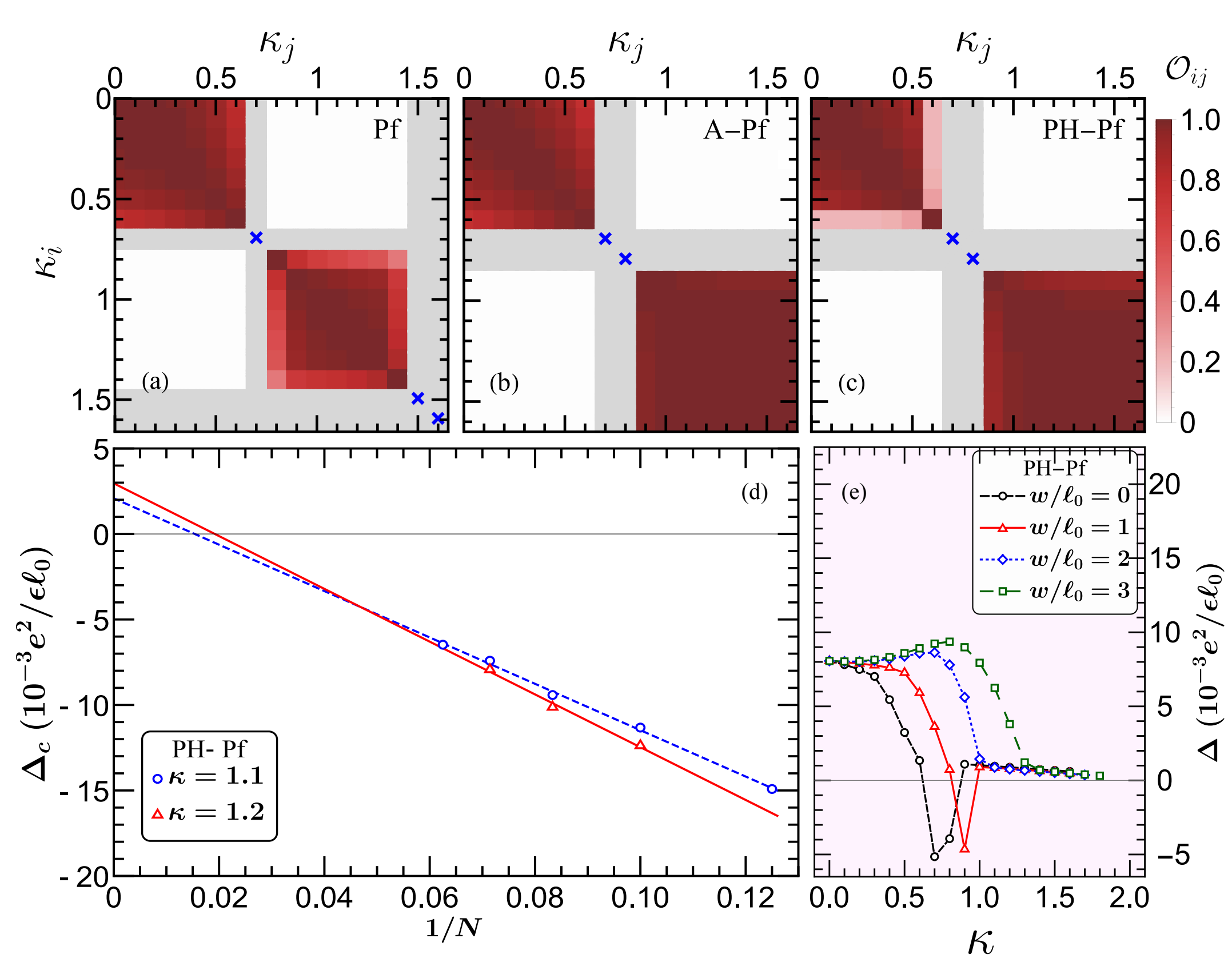
- ❖ Normalized thermal conductance coefficient $K = (2.53 \pm 0.04)\kappa_0$ for $T_0 = 18 - 25$ mK
- ❖ $T_0 \leq 15$ mK \Rightarrow increase of equilibration length of counter propagating modes $\Rightarrow K$ rises

Shot Noise Experiment^[4]

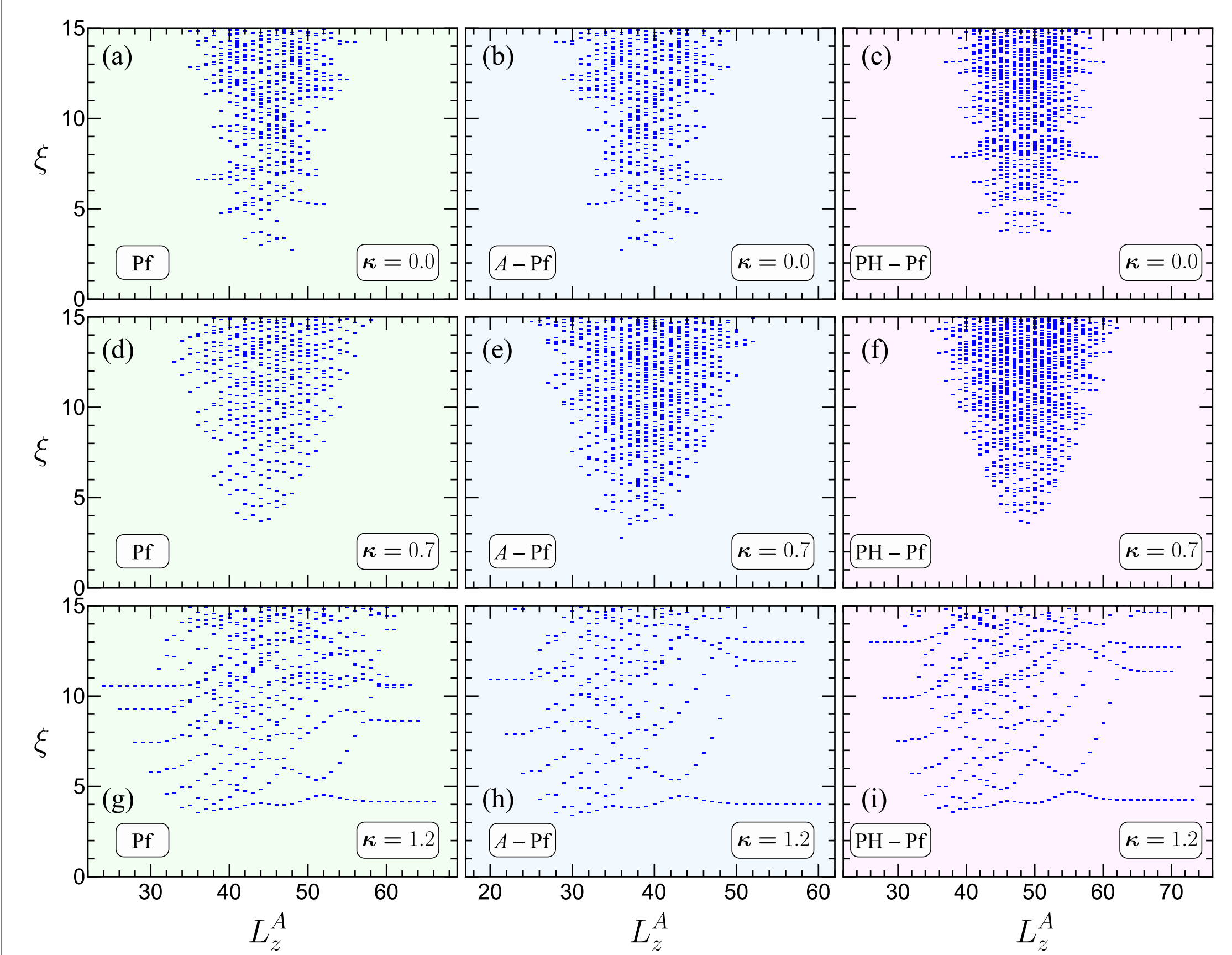


- Measurement of Down stream noise at the interface of $\nu = 5/2$ and $\nu = 3$,
- ❖ PH-Pf: DOWN stream Majorana mode \Rightarrow Noise
 - ❖ A-Pf: UP stream Majorana mode \Rightarrow NO Noise

LANDAU LEVEL MIXING - EMERGENCE OF ANOMALOUS PHASE (A-PHASE)



- Fig (a)-(c), exact overlap matrix, $O_{ij} = \langle \Psi_{\text{ex}}(\kappa_i) | \Psi_{\text{ex}}(\kappa_j) \rangle$ for Pf, A-Pf, PH-Pf at $N = 14, 12, 14$ respectively
- Blue crosses \Rightarrow unquantized points; Gray zones \Rightarrow unquantized regime
- Finite charge gap, Δ_c for PH-Pf at thermodynamic limit
- Finite neutral excitation gap, Δ for PH-Pf at high- κ
- $\kappa \sim 0.7-1.5 \Rightarrow$ **Reentrant Anomalous Phase**
- **Experimental Regime**



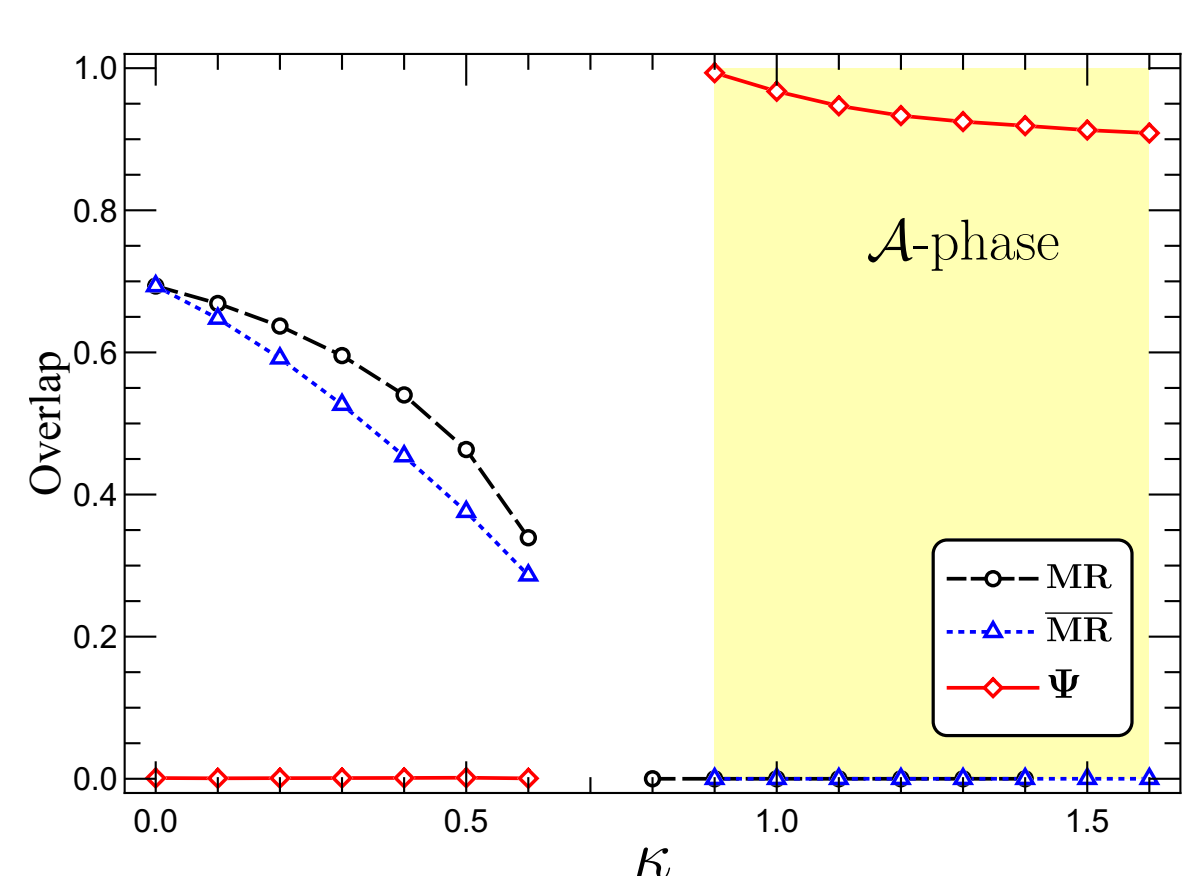
- Fig (a)-(i) Entanglement spectra of exact states of Pf, A-Pf, PH-Pf fluxes for different κ sectors
- Well gapped ES in the A-phase
- Close similarities of ES in the A-phase \Rightarrow Unique topological order irrespective of different flux

PROPOSED WAVE FUNCTION FOR 5/2 STATE IN THE A-PHASE

$$\Psi = J_N \mathcal{S} \left[\prod_{1 \leq i, j \leq N/2} (z_i - z_{N/2+j})^2 \right]$$

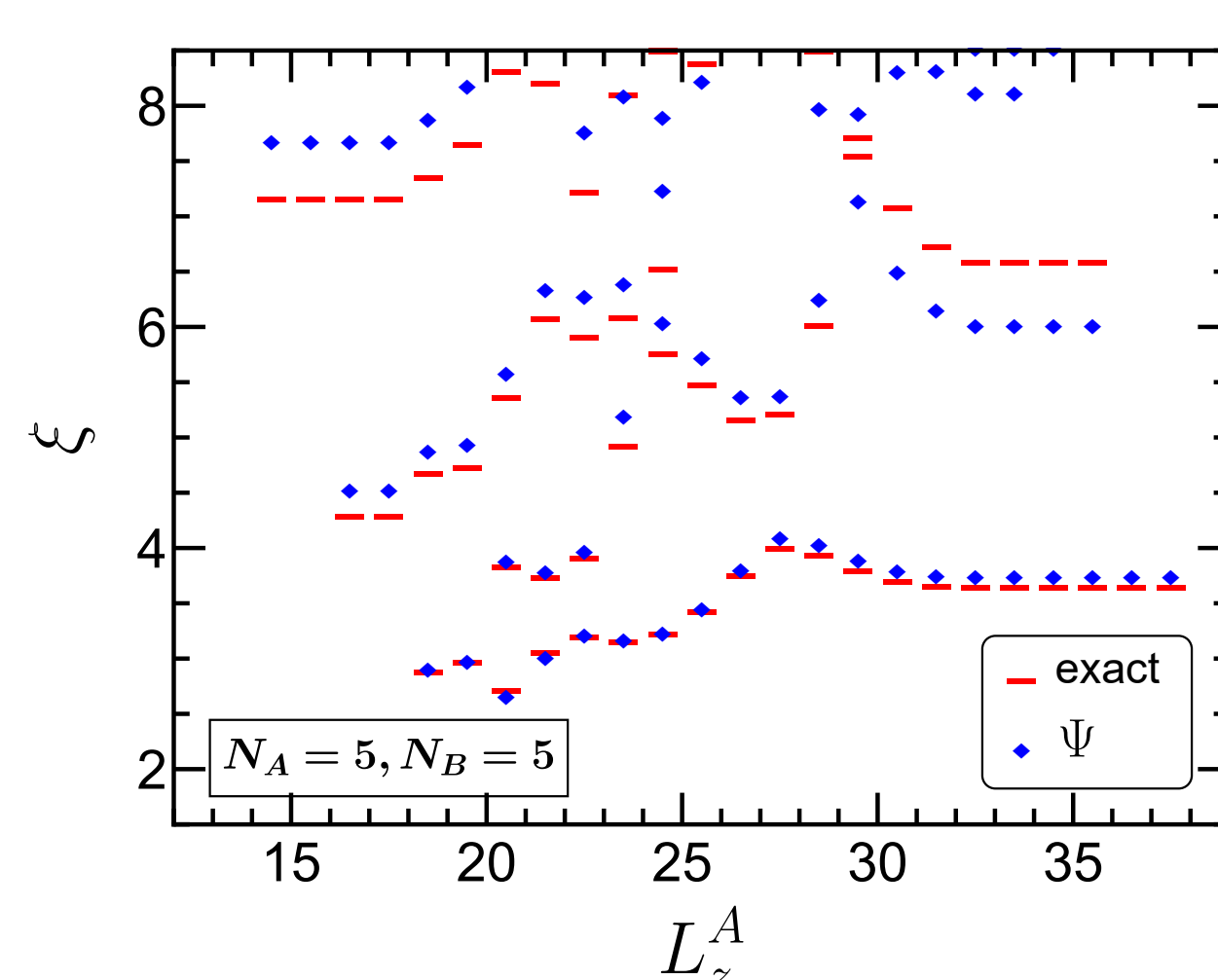
- ❖ $J_N = \prod_{i < j} (z_i - z_j)$ is the N -particle Jastrow factor; z_i electronic coordinates.
- ❖ Two **Bose-Einstein condensates** of non-interacting composite bosons consisting $N/2$ -particles with strong repulsion.
- ❖ Total flux = $2N - 1$ (PH-Pf)

OVERLAP



- ❖ In the lower κ -phase,
 - ❖ The overlaps of MR and $\overline{\text{MR}}$ decays with κ
 - ❖ Overlap of Ψ is zero
- ❖ In the A-phase,
 - ❖ The overlaps of MR and $\overline{\text{MR}}$ is zero
 - ❖ Overlap of Ψ is consistently very high

TOPOLOGICAL PROPERTIES



- ❖ Topological properties of Ψ is encoded in **K-matrix**,

$$\mathbf{K} = \begin{pmatrix} 1 & 3 \\ 3 & 1 \end{pmatrix}, \quad \vec{t} = \begin{pmatrix} 1 \\ 1 \end{pmatrix}, \quad \vec{s} = \begin{pmatrix} 1/2 \\ 1/2 \end{pmatrix}$$
- ❖ Filling factor, $\nu = \vec{t}^T \cdot \mathbf{K}^{-1} \cdot \vec{t} = 1/2$
- ❖ Shift = $(2/\nu) \vec{t}^T \cdot \mathbf{K}^{-1} \cdot \vec{s} = 1$
- ❖ Ground state degeneracy, $\mathcal{D} = |\text{Det}(\mathbf{K})^g| = 8^g$
- ❖ Eigen-values of \mathbf{K} : one +ve, one -ve \Rightarrow Central charge = 0
- ❖ Macroscopic $N/2$ bosons can sit together \Rightarrow coset group \mathbb{Z}_2 \Rightarrow possibly supports Majorana edge Mode
- ❖ Total central charge = $2 + 0 + 1/2 = 5/2$

SUMMARY

- ★ Our work finds a possible resolution to the earlier theoretical debate and experimental observation.
- ★ We have identified a reentrant anomalous phase, distinct from conventional Pf or A-Pf phase at an intermediate range of LLM.
- ★ We propose a wave function for this phase having similar flux of PH-Pf which possesses very high overlap and good matching of low-lying ES.
- ★ The unique topological order observed for this A-phase should possibly correspond to the experimentally observed phase.

References

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